



Millimeter-Wave Networks for Vehicular Communication: Modeling and Performance Insights

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- Why Should I Put Comms Onto Self-Driving Vehicles?
- ... and Why Should I go for mmWave Systems?
- Proposed mmWave V2I System Model
- Numerical Results
- Conclusions

mmWave Comms for Next Generation ITSs

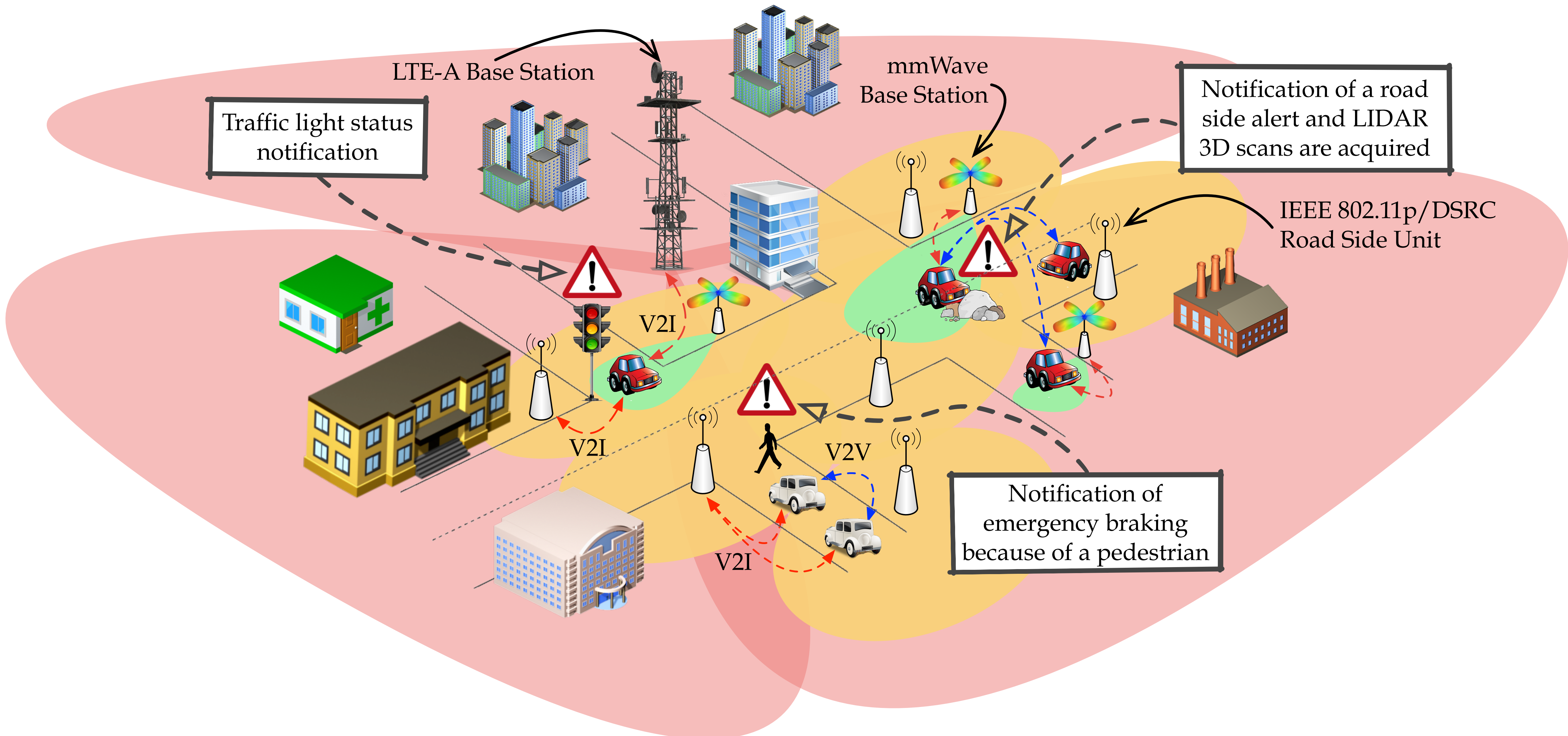


- The IEEE 802.11p/DSRC can achieve at most ~27 Mbps, in practice it is hard to observe that.
- However, DSRC standards are suitable for low-rate data services (for e.g., positioning beacon, emergency stop messages, etc.).
- On the other hand, future CAVs will require solutions ensuring gigabit-per-second communication links to achieve proper 'look-ahead' services (involving cameras, LIDARS, etc.), etc.
- It is reasonable to design hybrid networks integrating both mmWave and DSRC technologies



mmWave Comms for Next Generation ITSs

IEEE 802.11p/DSRC Coverage (Base Layers) LTE-A Coverage (1st Enhancement Layers) mmWave Coverage (2nd Enhancement Layers)



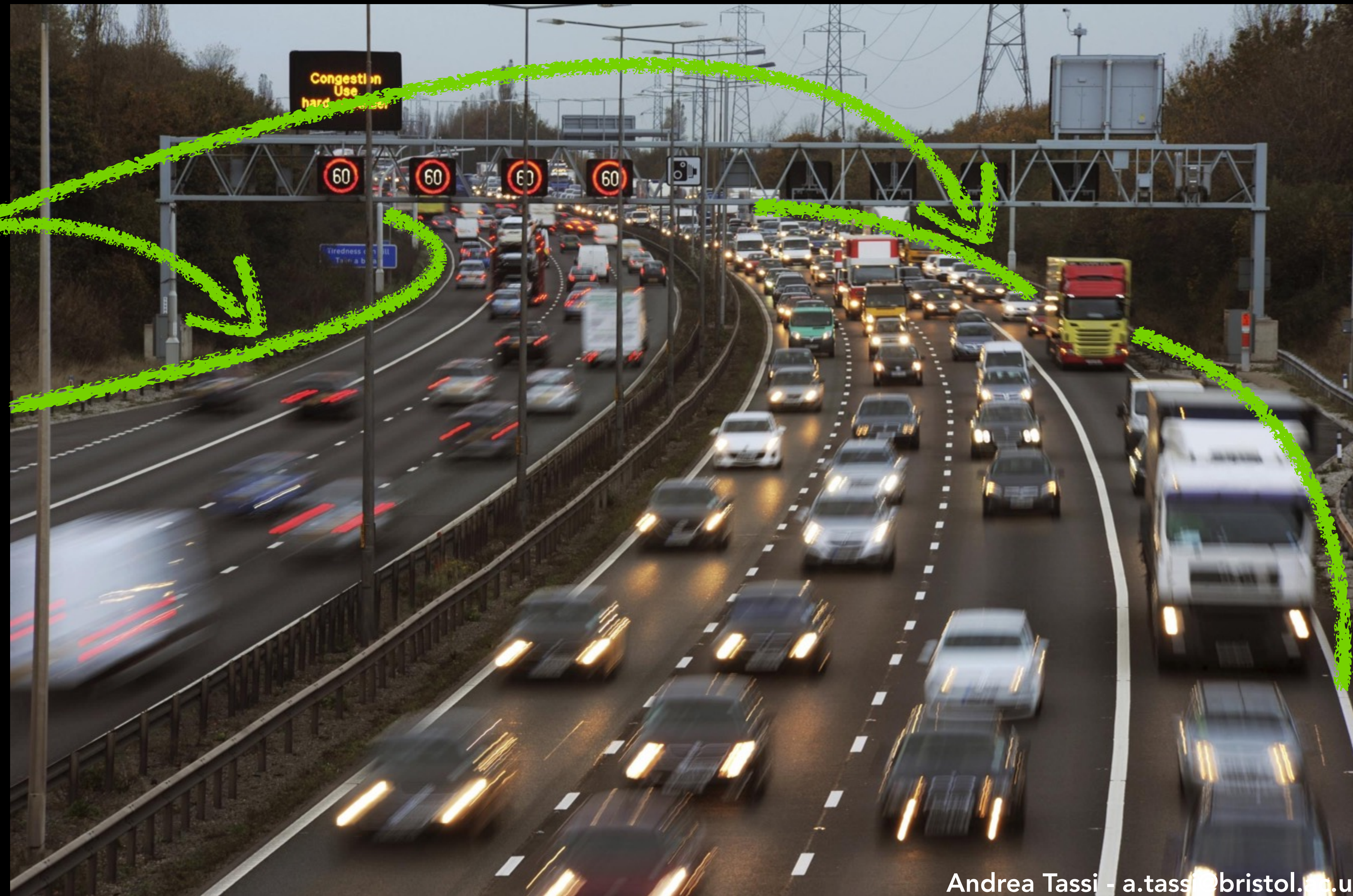


System Model

Practical Highway Scenario



mmWave BSs
placed at
the side of
the road

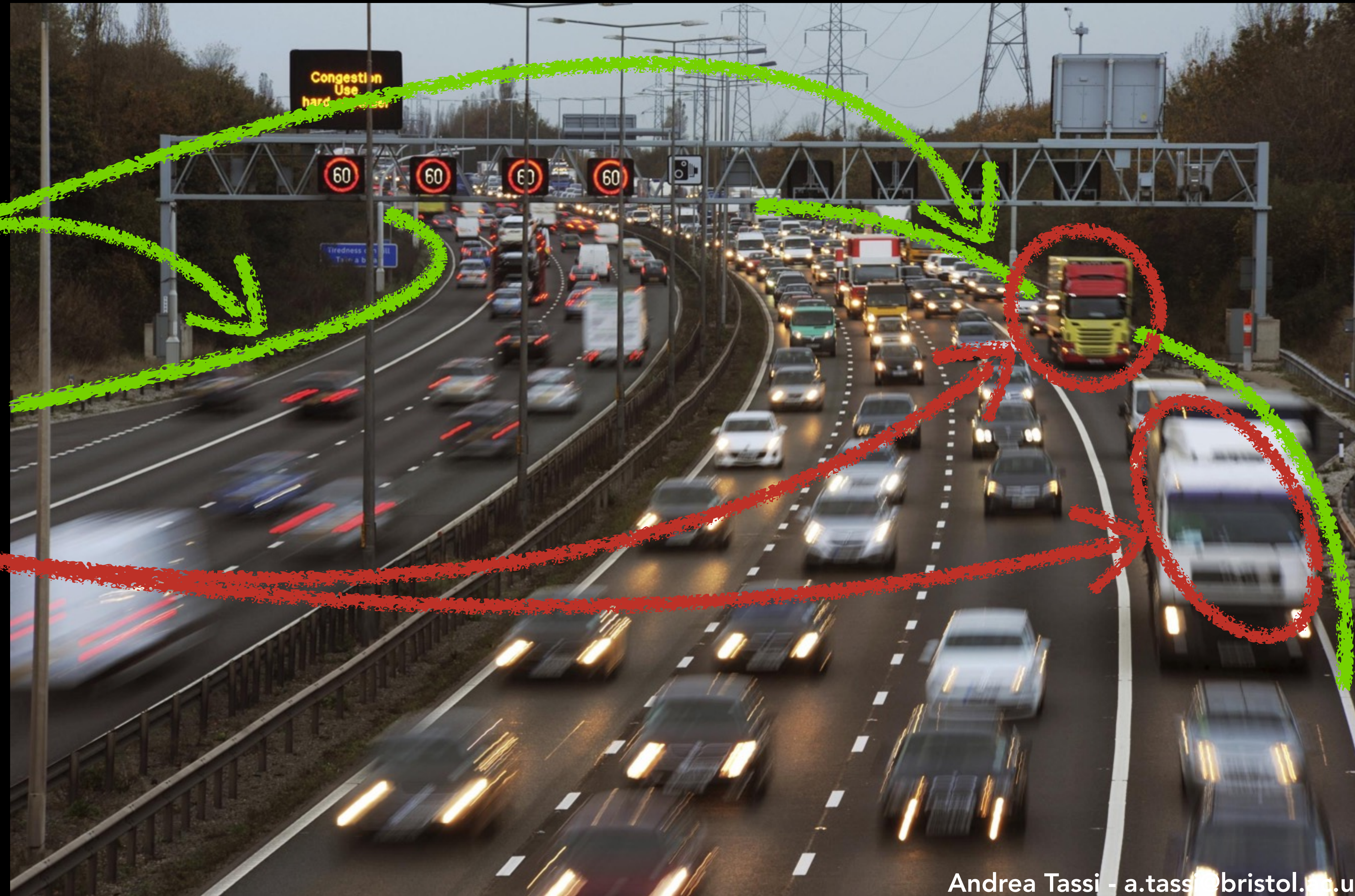




Practical Highway Scenario

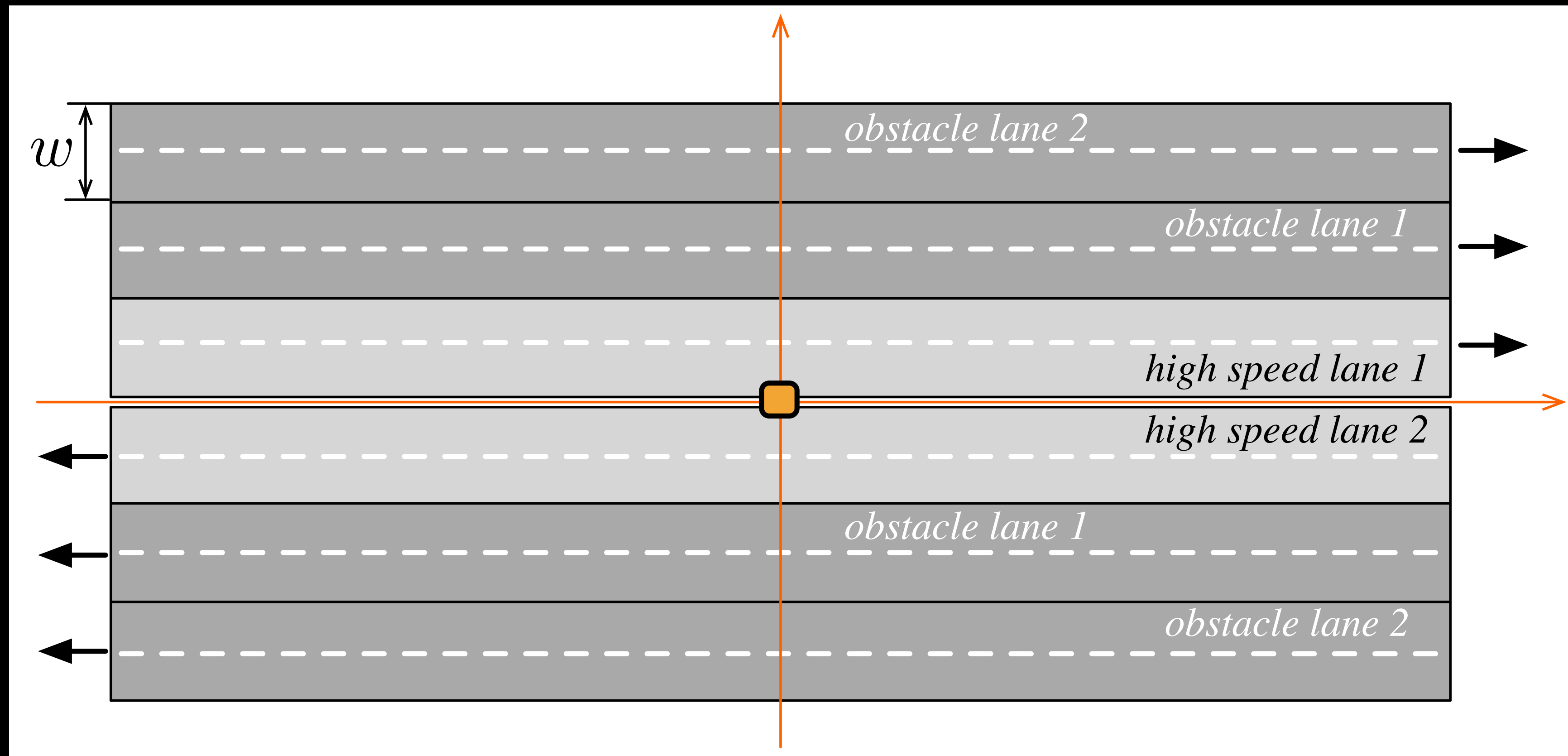
mmWave BSs
placed at
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Obstacles





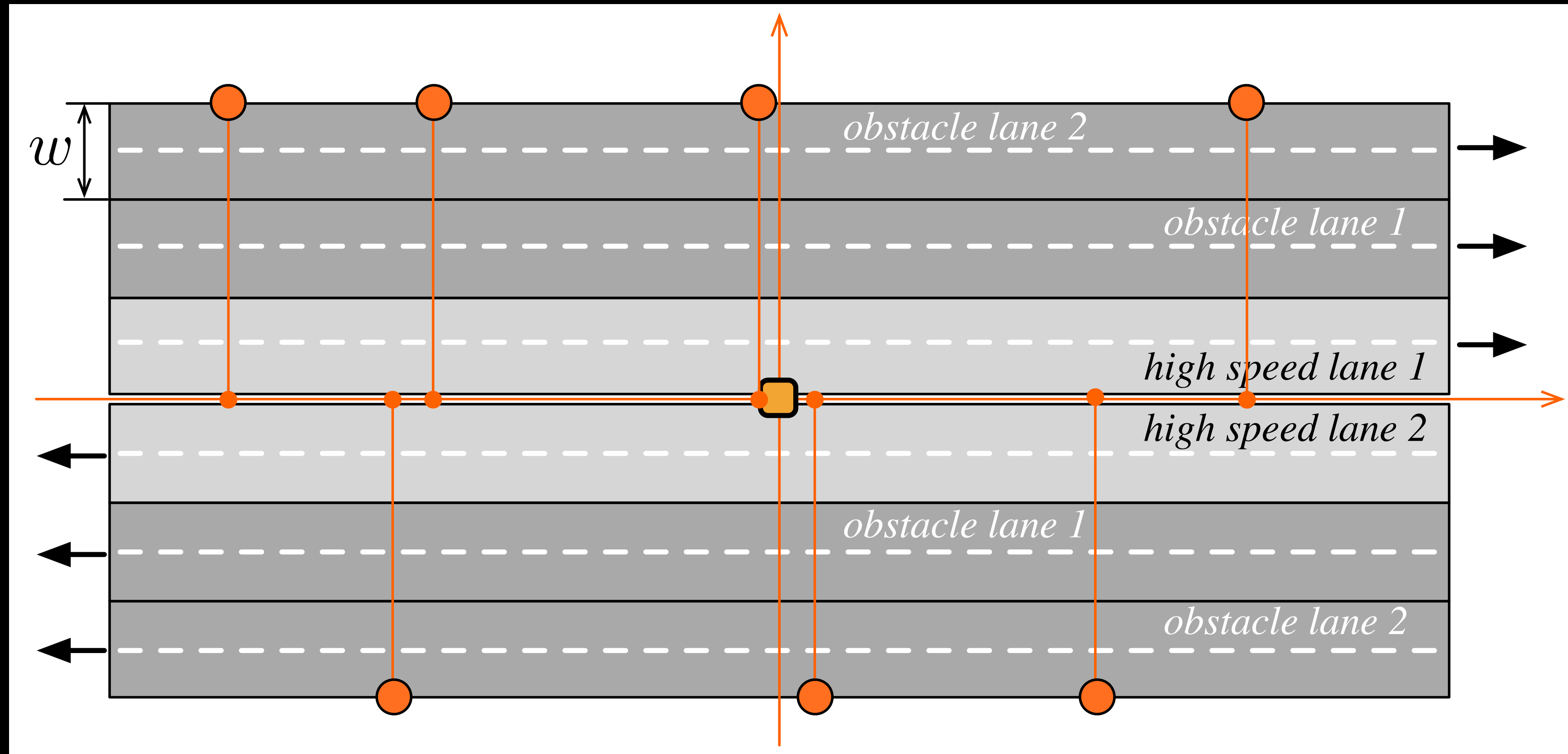
System Model (Road Layout)



- Straight and **homogeneous** road section
- Vehicles are required to drive on the **left hand side of the road**
- We characterize the performance of a **standard user placed at the origin of the axis.**



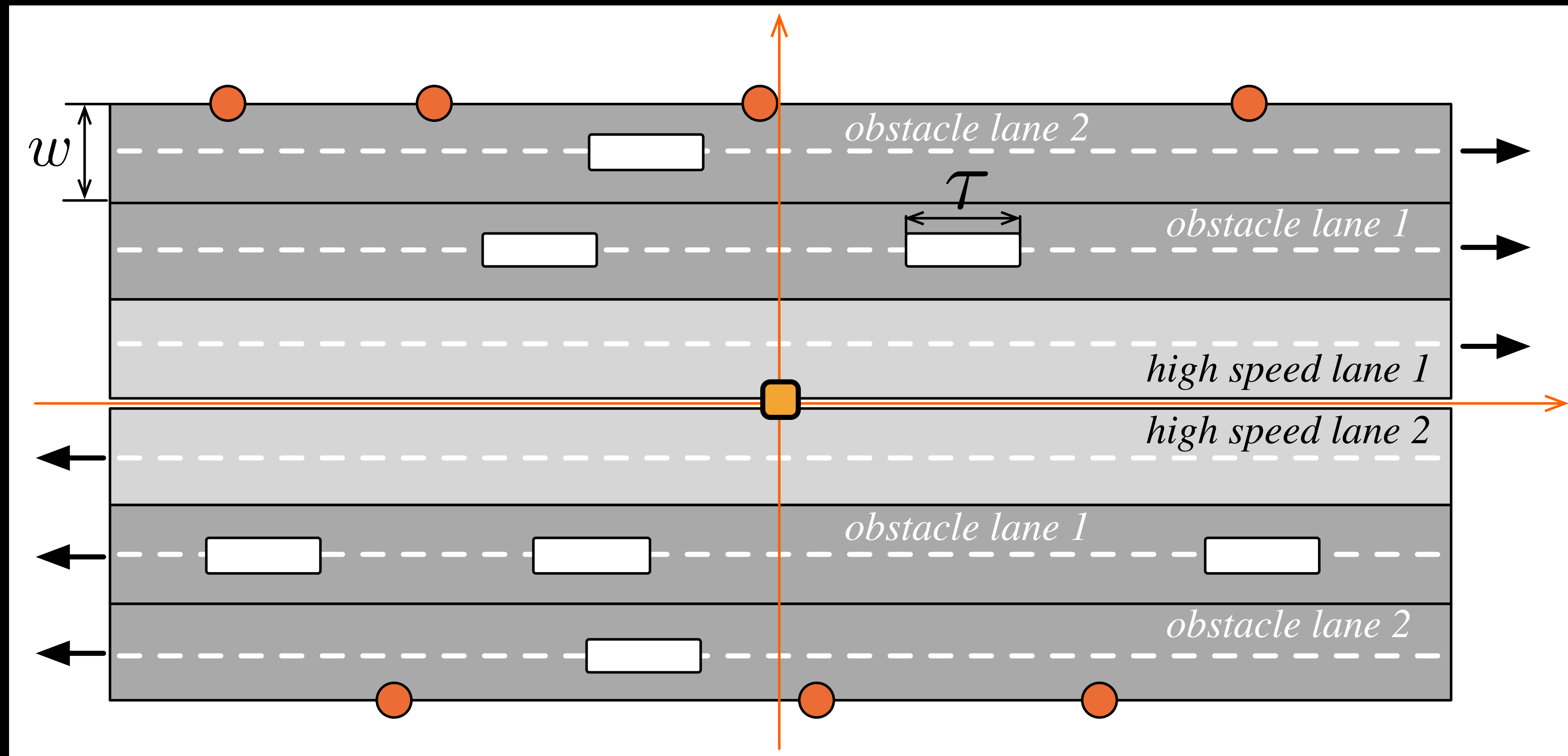
System Model (BS Distribution)



- x -comp. of **BS positions** follow a **1D PPP** of density λ_{BS}
- A BS is placed on a side of the road (upper/bottom side) with probability $q = 0.5$. Hence, BSs on a side of the road define a 1D PPP of density $q\lambda_{BS}$



System Model (Blockage Distribution)

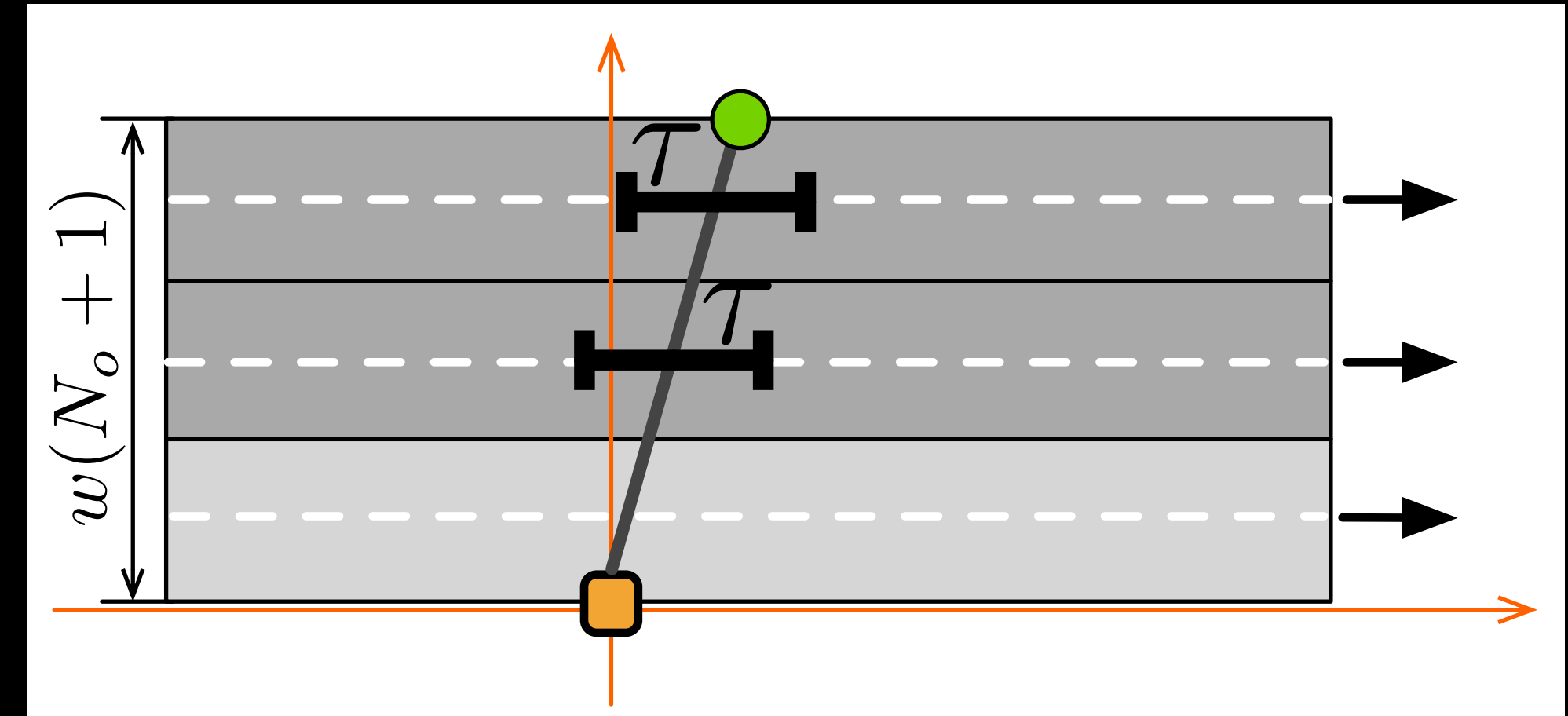
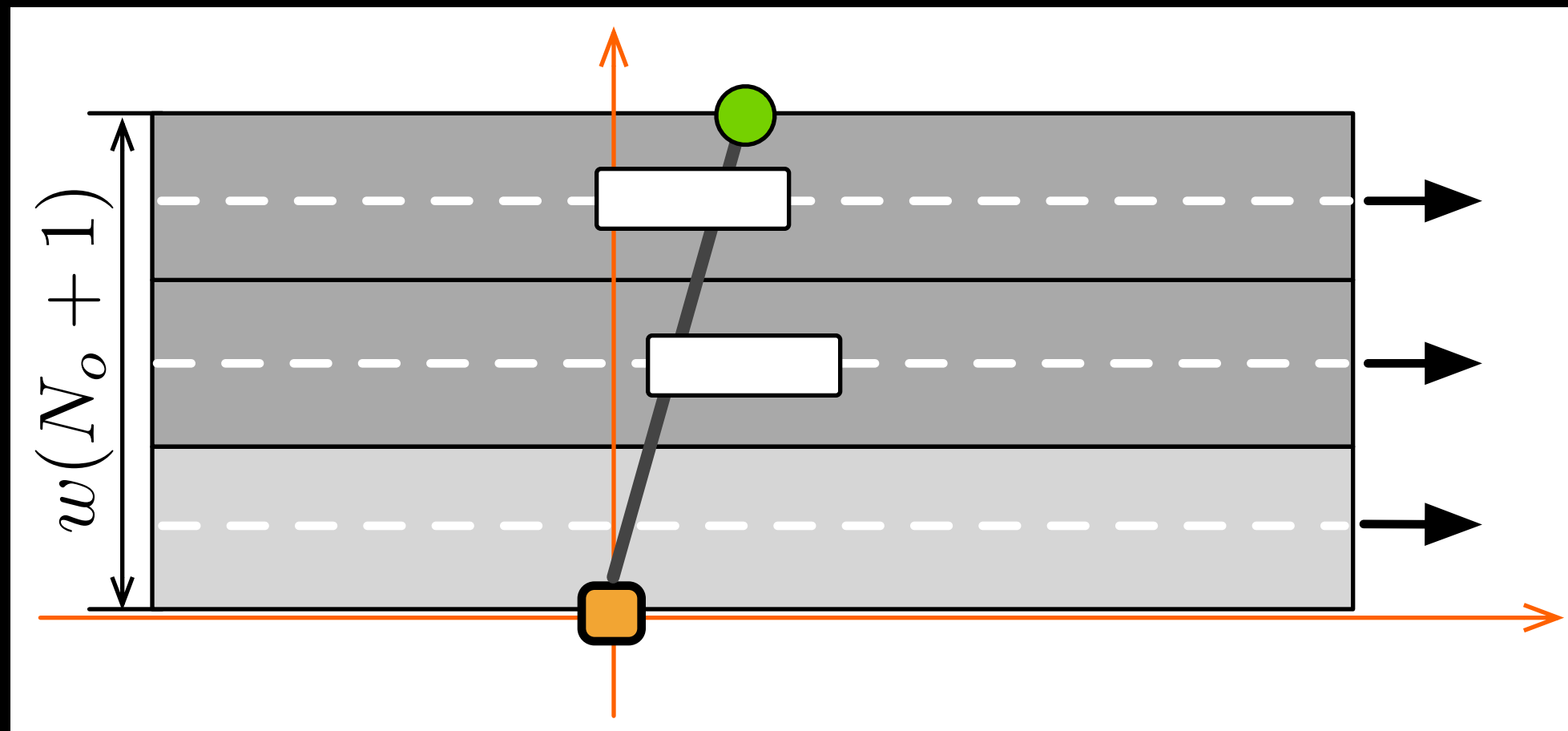


- Obstacles on each obstacle lane follow a 1D PPP of density $\lambda_{o,\ell}$
- **Obstacle processes are independent** but the blockage density of lane ℓ on each traffic direction is the same
- Each blockage is associated with a **footprint** of length τ



PL Model and User Association

- We approximate p_L with the probability that no blockages are present within a distance of $\tau/2$ on either side of the ray connecting the user to a BS. Hence, our approximation is independent on the distance of BS i to O



- The PL function associated with BS i is

$$\ell(r_i) = \mathbf{1}_{i,L} C_L r_i^{-\alpha_L} + (1 - \mathbf{1}_{i,L}) C_N r_i^{-\alpha_N}$$

- The standard user always connects to the BS with the minimum PL component



PL Model and User Association

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#Obs. Lane per driving direction

$$p_L \cong \prod_{\ell=1}^{N_o} e^{-\lambda_{o,\ell}\tau}$$

1D PPP void probability

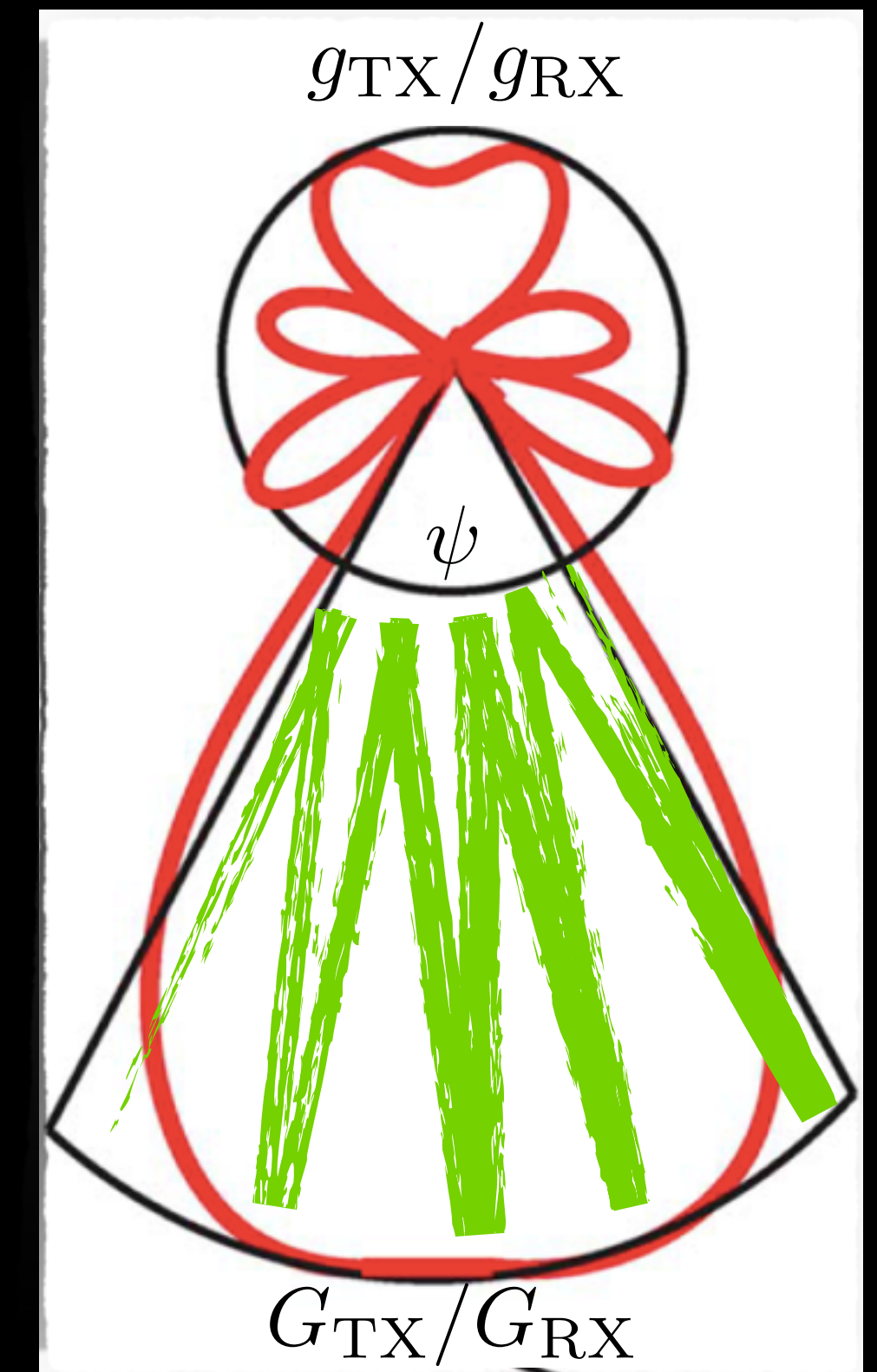
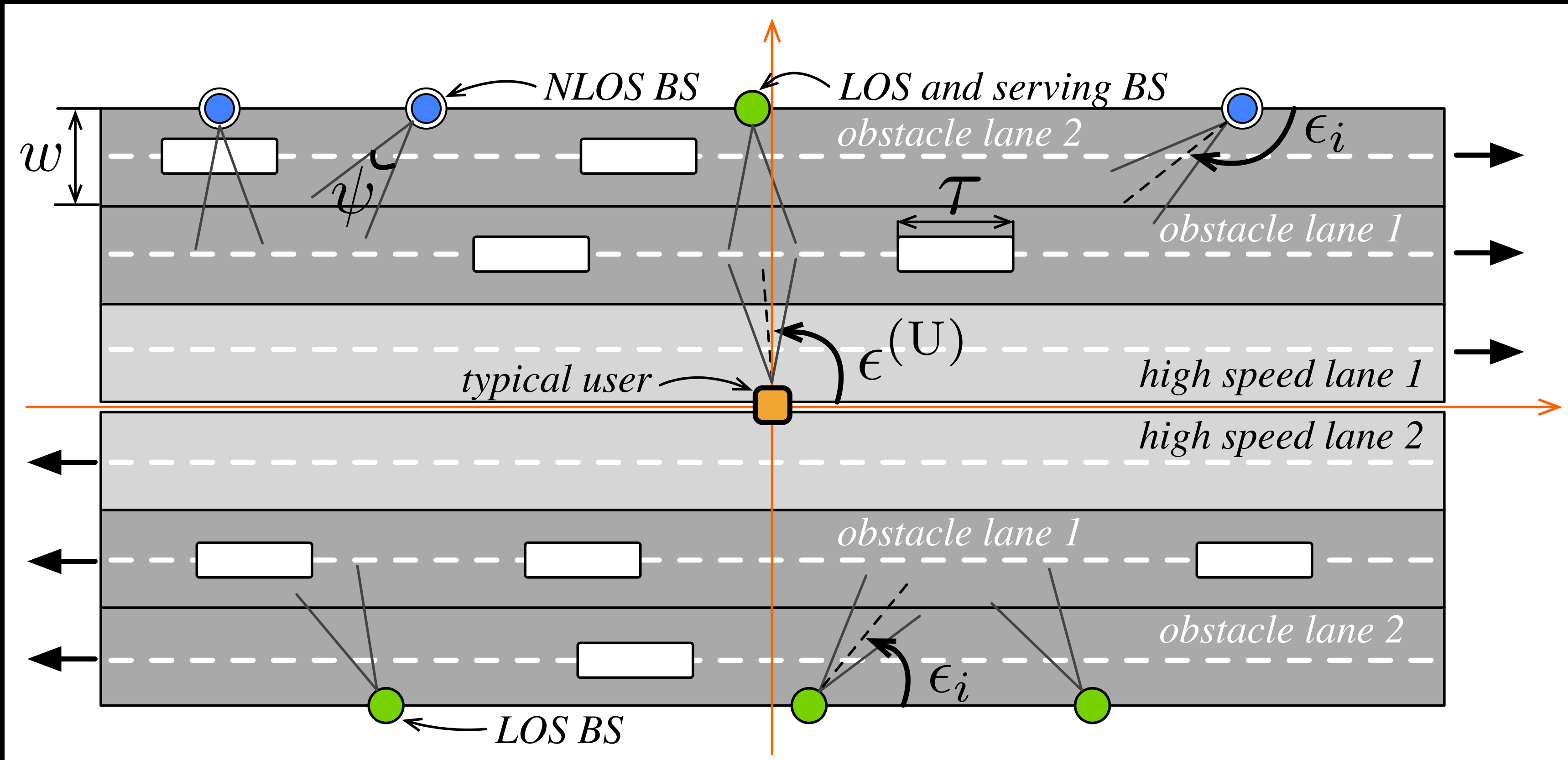
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System Model (Beam Steering)



- The main lobe of each BS is always entirely directed towards the road
- The user/BS beam alignment is assumed error-free
- The beam on an interfering BS is steered uniformly within 0° and 180°



SINR Outage and Rate Coverage





The Probability Framework

- Assume the user connects to BS 1, we define the **SINR** as

$$\text{SINR}_O = \frac{h_1 \Delta_1 \ell(r_1)}{\sigma + \sum_{j=2}^b h_j \Delta_j \ell(r_j)}$$

normalized thermal noise power

antenna gains

$h_j \sim \text{EXP}(1)$



The Probability Framework

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normalized thermal noise power
antenna gains
 $h_j \sim \text{EXP}(1)$

- We characterize the following **SINR outage**

$$\underbrace{\mathbb{P}[\text{SINR}_O < \theta]}_{P_T(\theta)} = P_L - \underbrace{\mathbb{P}[\text{SINR}_O > \theta \text{ and std. user served in LOS}]}_{P_{CL}(\theta)} + P_N - \underbrace{\mathbb{P}[\text{SINR}_O > \theta \text{ and std. user served in NLOS}]}_{P_{CN}(\theta)}$$



Probability of Being Served in LOS/NLOS

- The standard user connects to a **NLOS BS** with probability

$$P_N = \int_{w(N_o+1)}^{\infty} f_N(r) e^{-2\lambda_L \sqrt{A_L^2(r) - w^2(N_o+1)^2}} dr$$

PDF of the closest
NLOS BS

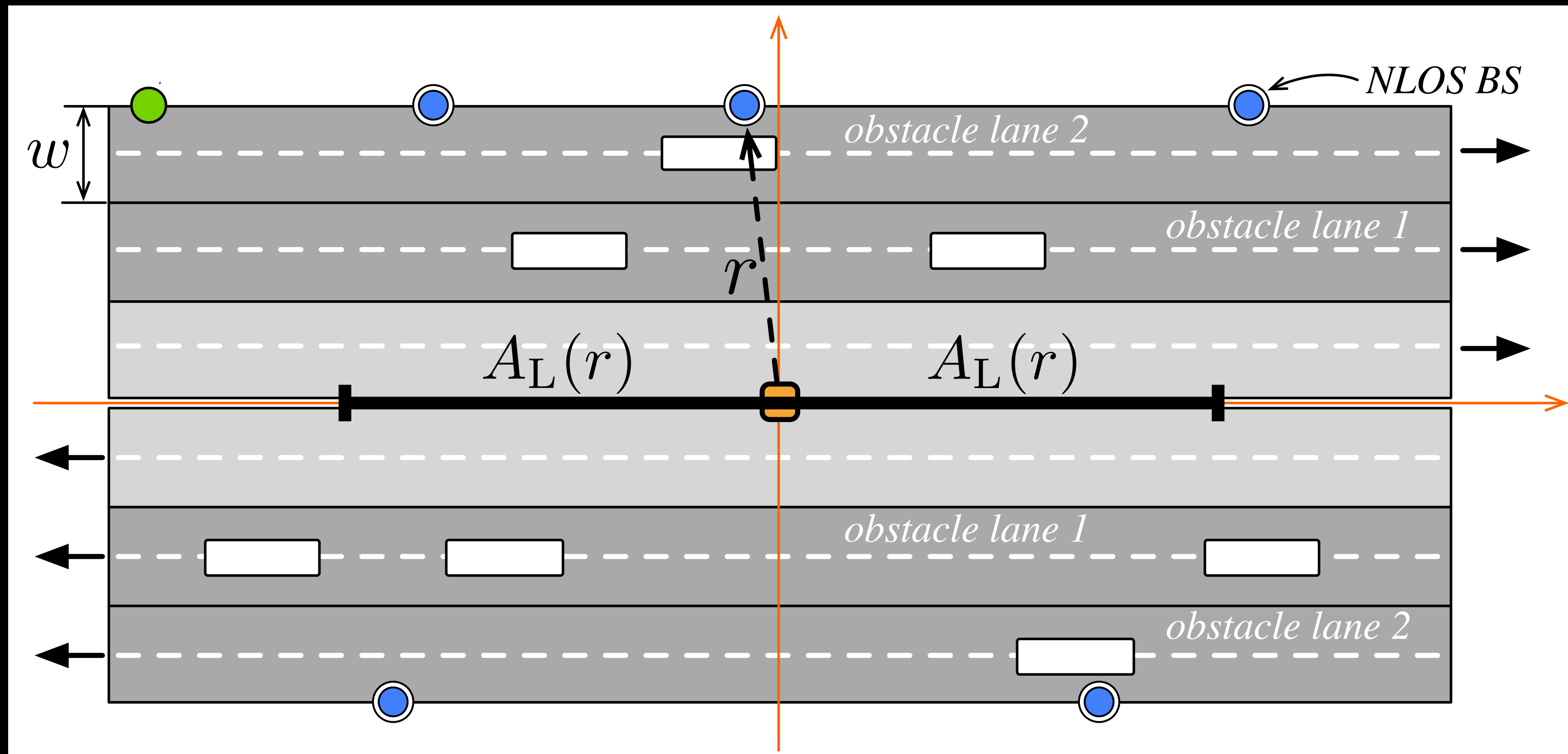
PPP LOS void probability in
the segment $[0, A_L(r)]$



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where

$$A_L(r) = \max \left\{ w(N_o + 1), \left[\frac{C_N}{C_L} r^{-\alpha_N} \right]^{-\frac{1}{\alpha_L}} \right\}$$

from $C_N r^{-\alpha_N} = C_L A_L^{-\alpha_L}$

- While, $P_L = 1 - P_N$



Coverage Probability Terms

$$\underbrace{\mathbb{P}[\text{SINR}_O < \theta]}_{P_T(\theta)} = P_L - \underbrace{\mathbb{P}[\text{SINR}_O > \theta \text{ and std. user served in LOS}]}_{P_{CL}(\theta)} + P_N - \underbrace{\mathbb{P}[\text{SINR}_O > \theta \text{ and std. user served in NLOS}]}_{P_{CN}(\theta)}$$



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Coverage Probability Terms

$$P_{\text{CL}}(\theta) = \mathbb{P} \left[\frac{h_1 \Delta_1 \ell(r_1)}{\sigma + I} > \theta \text{ and std. user is served in LOS} \right]$$

as $h_1 \sim \text{EXP}(1)$

$$\stackrel{(i)}{=} \mathbb{E}_I \int_{w(N_o+1)}^{+\infty} e^{-\frac{(\sigma+I)\theta}{\Delta_1 C_L} r_1^{\alpha_L}} f_L(r_1) F_N(A_N(r_1)) dr_1$$

$$\stackrel{(ii)}{=} \int_{w(N_o+1)}^{+\infty} e^{-\frac{\sigma\theta}{\Delta_1 C_L} r_1^{\alpha_L}} \mathcal{L}_{I,L} \left(\frac{\theta r_1^{\alpha_L}}{\Delta_1 C_L} \right) f_L(r_1) F_N(A_N(r_1)) dr_1$$

Expectation w.r.t I Prob. of not being served in NLOS



Coverage Probability Terms

$$\overbrace{\mathbb{P}[\text{SINR}_O < \theta]}^{P_T(\theta)} = \overbrace{P_L - \mathbb{P}[\text{SINR}_O > \theta \text{ and std. user served in LOS}]}^{P_{CL}(\theta)} + \overbrace{P_N - \mathbb{P}[\text{SINR}_O > \theta \text{ and std. user served in NLOS}]}^{P_{CN}(\theta)}$$

- As α_N increases, in order to be convenient, a NLOS BS has to be quite close to O. Up to a point where P_L is (almost) 1. If so,

$$P_T(\theta) \cong 1 - \int_{w(N_o+1)}^{+\infty} e^{-\frac{\theta \sigma}{\Delta_1 C_L} r_1^{\alpha_L}} \mathcal{L}_{I,L} \left(\frac{\theta r_1^{\alpha_L}}{\Delta_1 C_L} \right) f_L(r_1) dr_1$$



Coverage Probability Terms

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- The rate coverage follows from the Fubini's theorem (for a bandwidth W)

$$R_C(\kappa) = 1 - P_T(2^{\kappa/W} - 1)$$



$\mathcal{L}_I(s)$
at a glance...



A Fundamental Result

- We proved that the Laplace transform of the interference component generated by the BSs on the upper/bottom side of the road ($S = U, S = B$) that are in LOS/NLOS with the user ($E = L, E = N$) can be approximated as

$$\mathcal{L}_{I_{S,E},\mathbb{E}_1}(s) \cong \prod_{\substack{S_1 \in \{U,B\}, \\ (a,b,\Delta) \in \mathcal{C}_{|\mathbf{x}_1|,S_1,\mathbb{E}_1,S,E}}} \sqrt{\mathcal{L}_{I_{S,E},\mathbb{E}_1}(s; a, b, \Delta)}$$

Conditioned of being served in LOS/NLOS ($\mathbb{E}_1 = L, \mathbb{E}_1 = N$).

- Where the fundamental Laplace transform term is...



A Fundamental Result

$$\mathcal{L}_{\text{IS},\text{E},\text{E}_1}(s; a, b, \Delta) \cong \exp \left(- \left(\mathbb{E}_h[\Theta(h, \Delta)] + \mathbb{E}_h[\Lambda(h, \Delta)] \right) \right)$$

$$\mathbb{E}_h [\Theta(h, \Delta)] = 2q\lambda_{\text{E}} \left[x^{-\alpha_{\text{E}}^{-1}} \left(1 - \frac{1}{s\Delta x + 1} \right) \right]_{x=a^{-\alpha_{\text{E}}}}^{b^{-\alpha_{\text{E}}}}$$

$$\begin{aligned} \mathbb{E}_h [\Lambda(h, \Delta)] &= -2q\lambda_{\text{E}}(s\Delta)^{\frac{1}{\alpha_{\text{E}}}} \left[t(-t^{-1})^{-\frac{1}{\alpha_{\text{E}}}} \Gamma \left(\frac{1}{\alpha_{\text{E}}} + 1 \right) \right. \\ &\quad \left. \cdot {}_2\tilde{F}_1 \left(\frac{1}{\alpha_{\text{E}}}, \frac{1}{\alpha_{\text{E}}} + 1; \frac{1}{\alpha_{\text{E}}} + 2; -t \right) \right]_{t=-(s\Delta a^{-\alpha_{\text{E}}} + 1)^{-1}}^{-(s\Delta b^{-\alpha_{\text{E}}} + 1)^{-1}} \end{aligned}$$



A Fundamental Result

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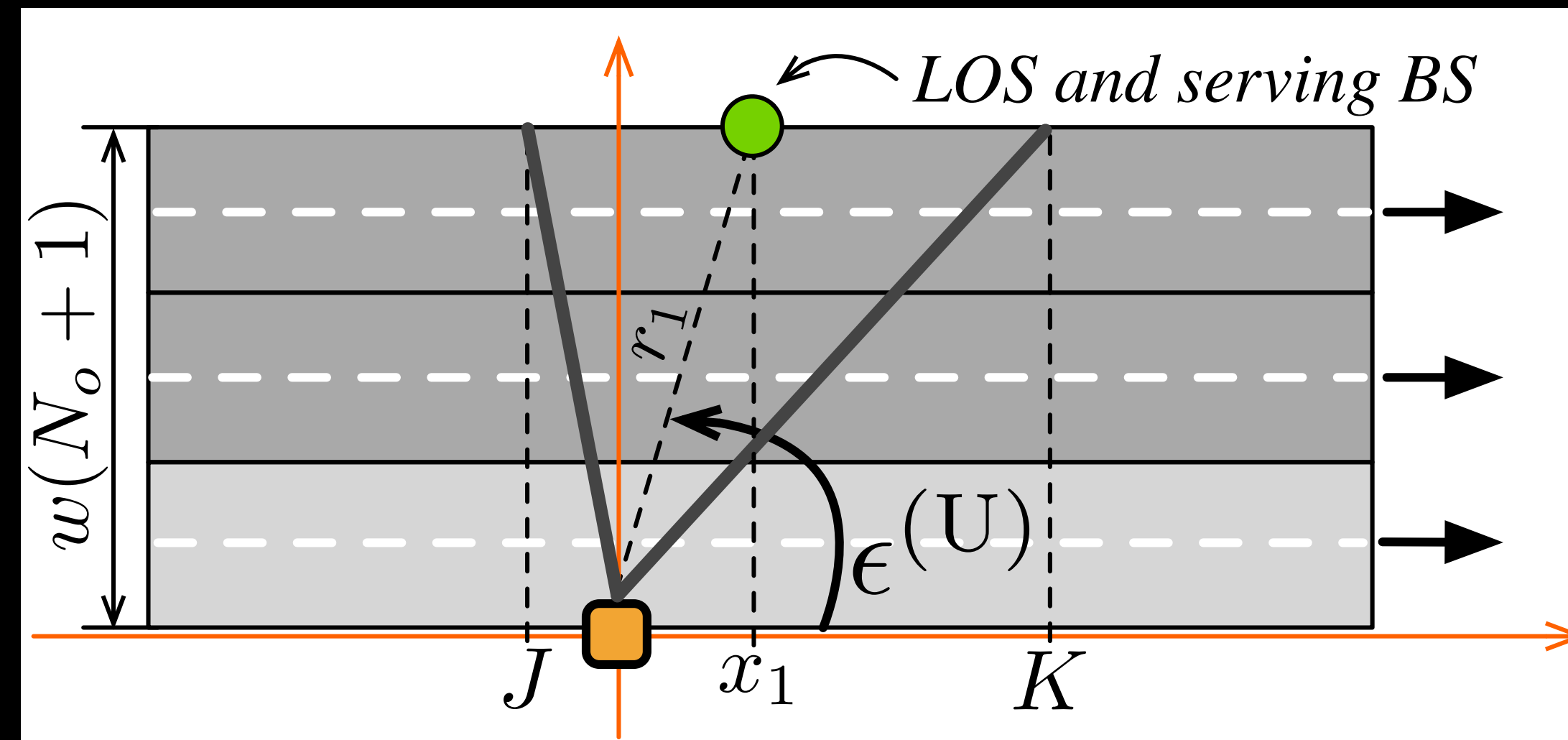
$$\mathbb{E}_h [\Theta(h, \Delta)] = 2q\lambda_E \left[x^{-\alpha_E^{-1}} \left(1 - \frac{1}{s\Delta x + 1} \right) \right]_{x=a^{-\alpha_E}}^{b^{-\alpha_E}}$$

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Parametrization of $\mathcal{L}_{\text{IS}, \text{E}, \mathbb{E}_1}$

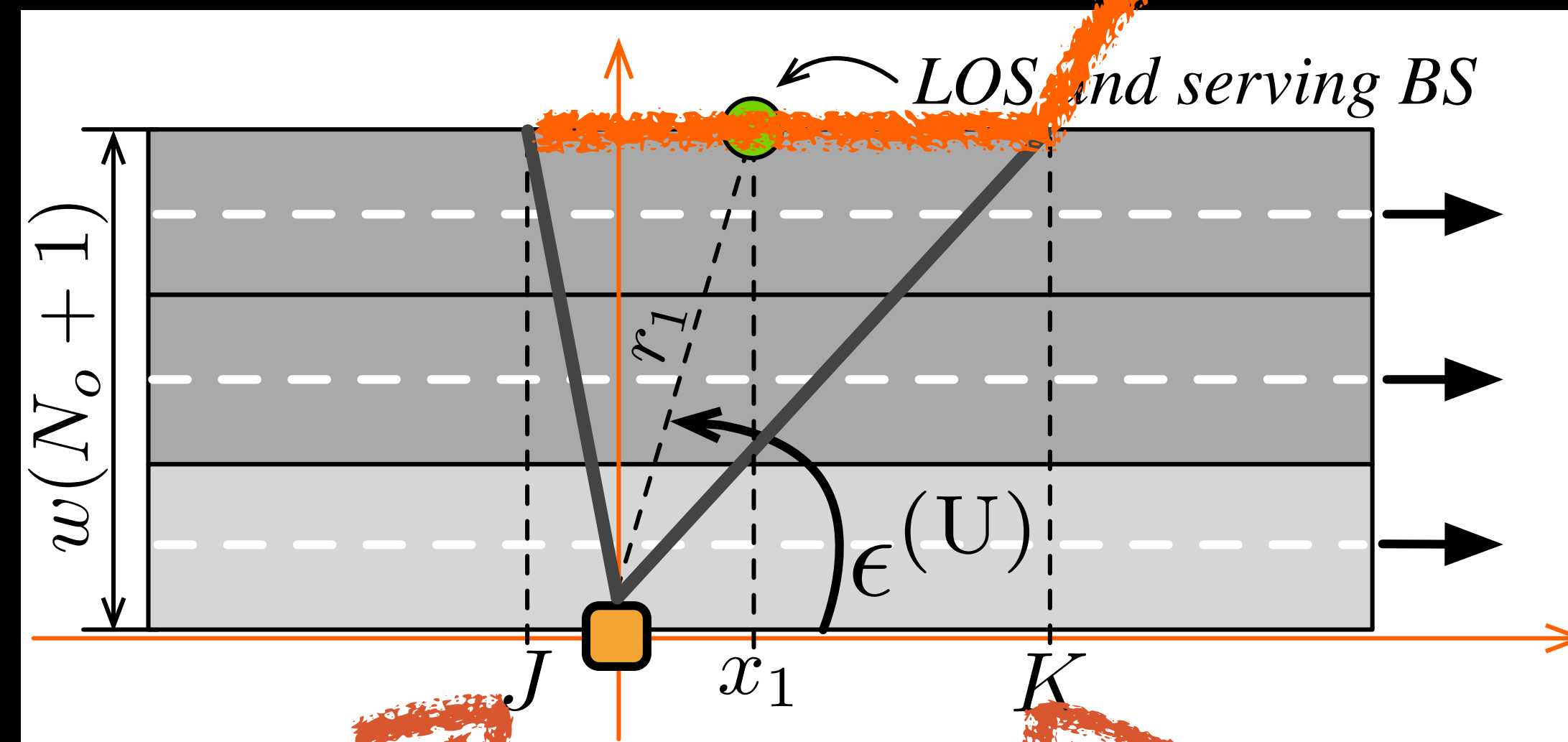
- For simplicity, we assume that the TX antenna gain is always equal to the minimum value.
- However, we characterize the RX antenna gain.





Parametrization of $\mathcal{L}_{\text{IS}, \mathbb{E}, \mathbb{E}_1}$

- For simplicity, we assume that the TX antenna gain is always equal to the minimum value.
- However, we characterize the RX antenna gain.



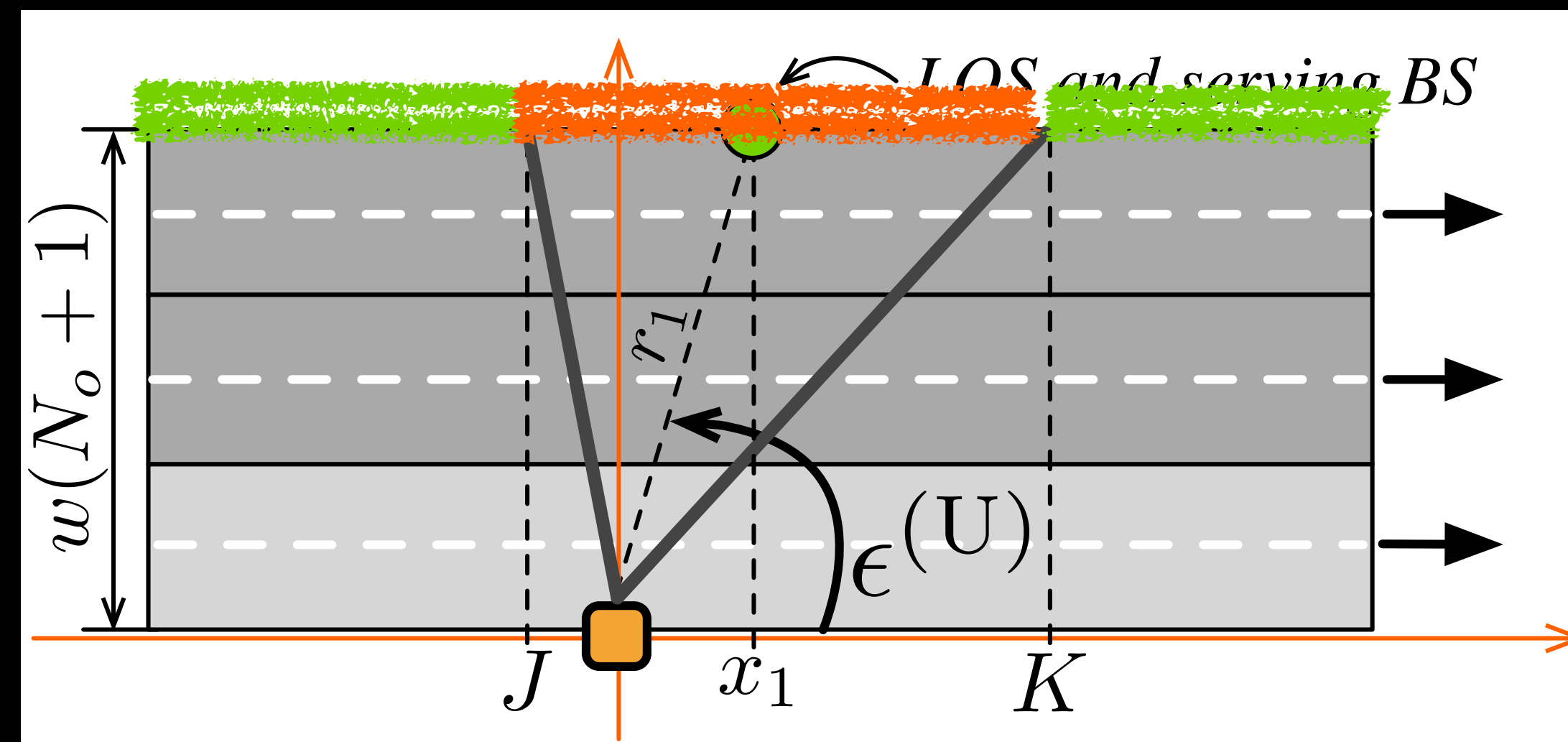
No other LOS BSs can be present in this interval



Parametrization of $\mathcal{L}_{\text{IS}, \text{E}, \mathbb{E}_1}$

- For simplicity, we assume that the TX antenna gain is always equal to the minimum value.
- However, we characterize the RX antenna gain.

Min RX gain
Max RX gain





Parametrization of $\mathcal{L}_{I_S, E, \mathbb{E}_1}$

$\langle S_1, \mathbb{E}_1, S, E \rangle$	Conditions on $ x_1 $	$(a, b, \Delta) \in \mathcal{C}_{ x_1 , S_1, \mathbb{E}_1, S, E}$
$\langle U, L, U, L \rangle$	For any $ x_1 $ such that $J > 0$	$(x_1 , K, g_{TX}G_{RX}),$ $(K, +\infty, g_{TX}g_{RX}),$ $(x_1 , +\infty, g_{TX}g_{RX})$
	For any $ x_1 $ such that $J \leq 0$	$(x_1 , K, g_{TX}G_{RX}),$ $(K, +\infty, g_{TX}g_{RX}),$ $(x_1 , J , g_{TX}G_{RX}),$ $(J , +\infty, g_{TX}g_{RX})$
$\langle U, L, U, N \rangle$	For any $ x_1 $ such that $J > 0$	$(x_N(r_1), J, g_{TX}g_{RX}),$ $(x_N(r_1), +\infty, g_{TX}g_{RX}),$ $(J, K, g_{TX}G_{RX}),$ $(K, +\infty, g_{TX}g_{RX})$
	For any $ x_1 $ such that $J \leq 0$	Refer to the case $\langle U, L, U, L \rangle$ ($J \leq 0$) and replace $ x_1 $ with $x_N(r_1)$
$\langle U, L, B, L \rangle$	For any $ x_1 $	$(x_1 , +\infty, g_{TX}g_{RX}),$ $(x_1 , +\infty, g_{TX}g_{RX}),$
$\langle U, L, B, N \rangle$	Refer to the case $\langle U, L, B, L \rangle$ and replace $ x_1 $ with $x_N(r_1)$	
$\langle U, N, U, L \rangle$	For any $ x_1 $ such that $x_L(r_1) > K$	Refer to the case $\langle U, L, B, L \rangle$ and replace $ x_1 $ with $x_L(r_1)$
	For any $ x_1 $ such that $x_L(r_1) \leq K$	Refer to the case $\langle U, L, U, L \rangle$ and replace $ x_1 $ with $x_L(r_1)$
$\langle U, N, U, N \rangle$	Refer to the case $\langle U, L, U, L \rangle$	
$\langle U, N, B, L \rangle$	Refer to the case $\langle U, L, B, L \rangle$ and replace x_1 with $x_L(r_1)$	
$\langle U, N, B, N \rangle$	Refer to the case $\langle U, L, B, L \rangle$	
Cases where $S_1 = B, S = B$	Refer to the correspondent cases where $S_1 = U$ and $S = U$	
Cases where $S_1 = B, S = U$	Refer to the correspondent cases where $S_1 = U$ and $S = B$	

- Finally, we can say

$$\mathcal{L}_{I, \mathbb{E}_1}(s) \cong \prod_{S \in \{U, B\}, E \in \{L, N\}} \mathcal{L}_{I_S, E, \mathbb{E}_1}(s)$$

- For e.g., if $\mathbb{E}_1 = L$ and $J > 0$, it follows

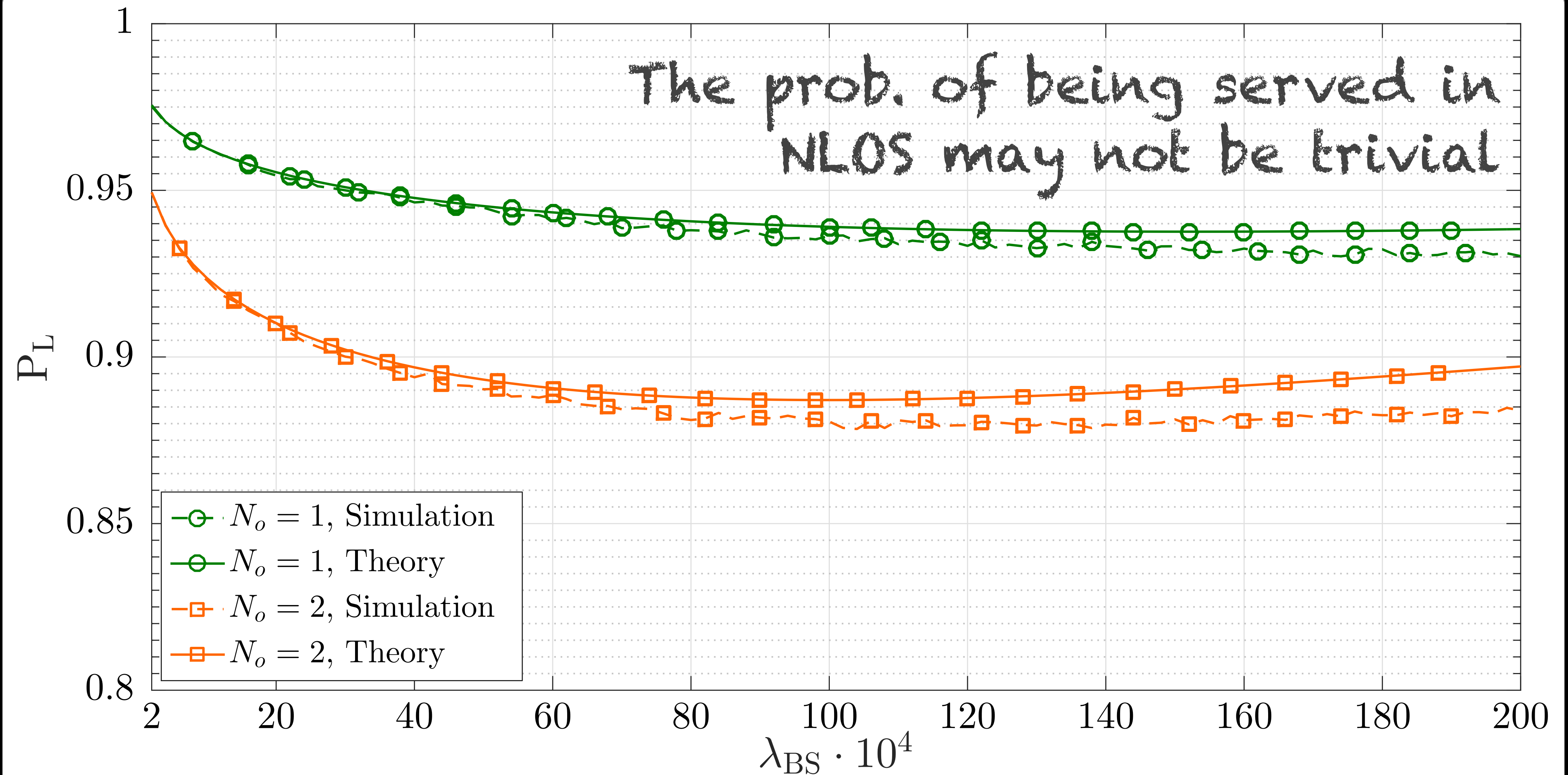
$$\begin{aligned} \mathcal{L}_{I, \mathbb{E}_1}(s) &\cong \mathcal{L}_{I_S, E, \mathbb{E}_1}(s; |x_1|, K, g_{TX}G_{RX}) \\ &\cdot \mathcal{L}_{I_S, E, \mathbb{E}_1}(s; x_N(r_1), J, g_{TX}g_{RX}) \\ &\cdot \mathcal{L}_{I_S, E, \mathbb{E}_1}(s; J, K, g_{TX}G_{RX}) \\ &\cdot \left(\mathcal{L}_{I_S, E, \mathbb{E}_1}(s; K, +\infty, g_{TX}g_{RX}) \right)^2 \\ &\cdot \left(\mathcal{L}_{I_S, E, \mathbb{E}_1}(s; |x_1|, +\infty, g_{TX}g_{RX}) \right)^3 \\ &\cdot \left(\mathcal{L}_{I_S, E, \mathbb{E}_1}(s; x_N(r_1), +\infty, g_{TX}g_{RX}) \right)^3 \end{aligned}$$



Numerical Results

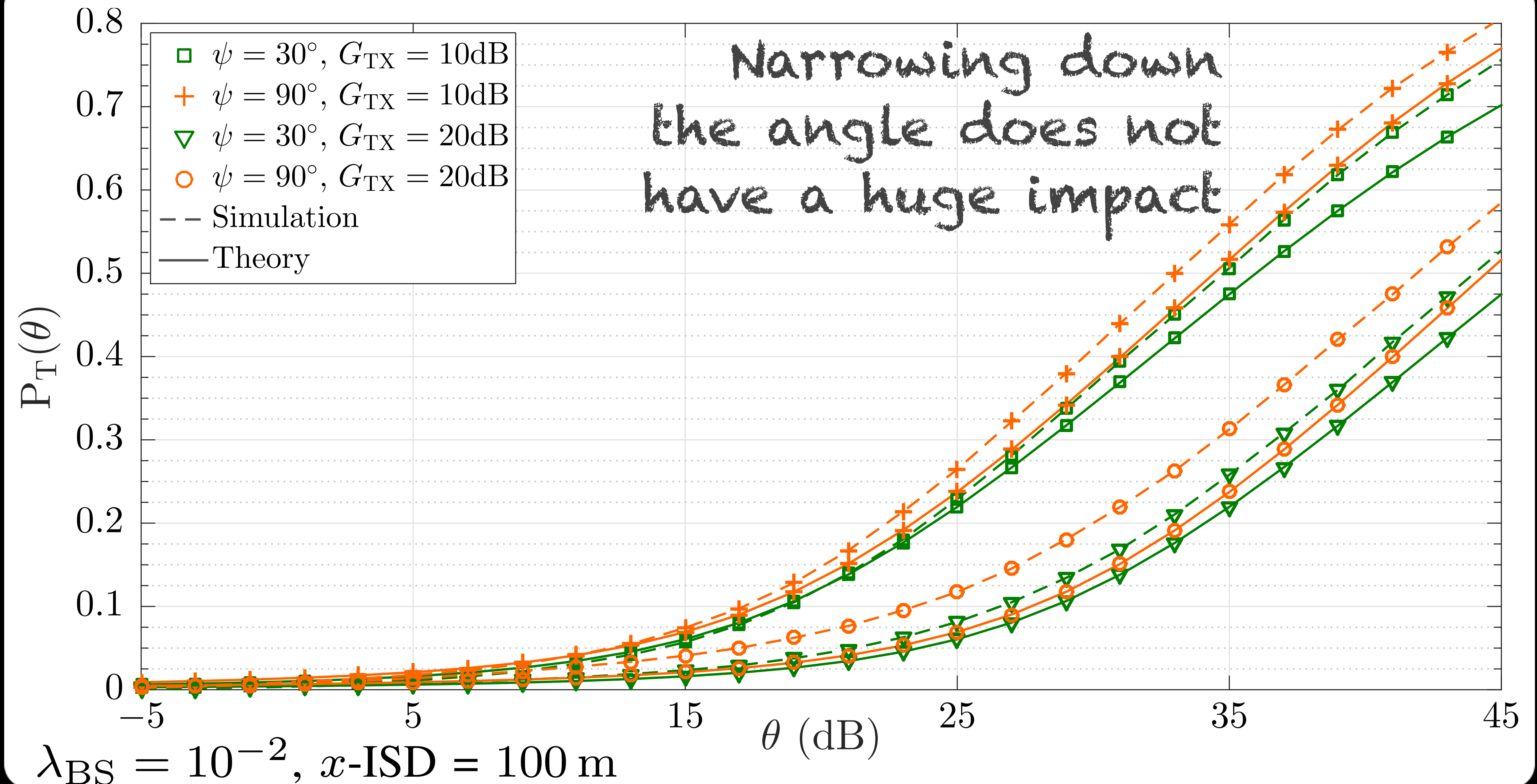


LOS vs. NLOS

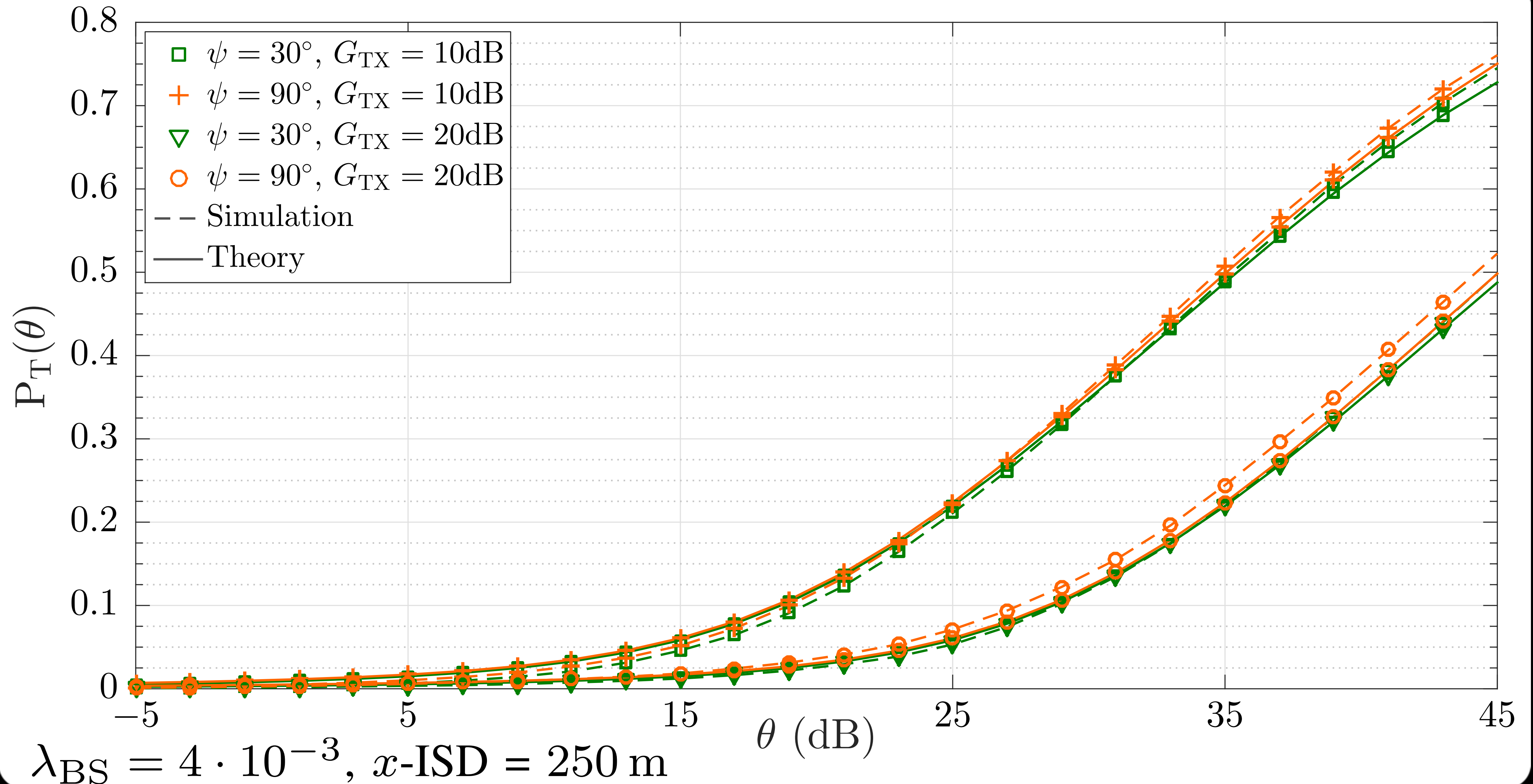




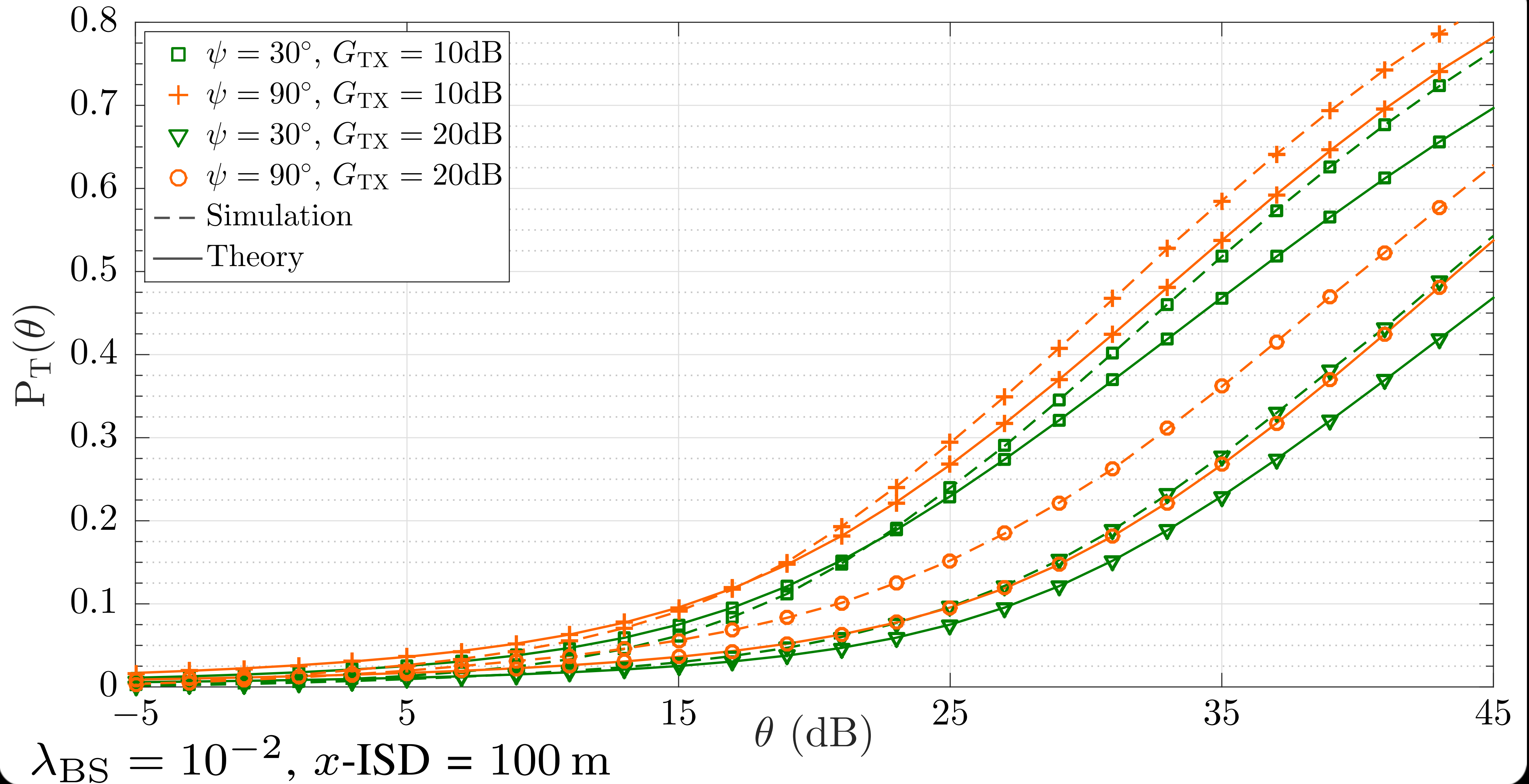
SINR Outage



SINR Outage

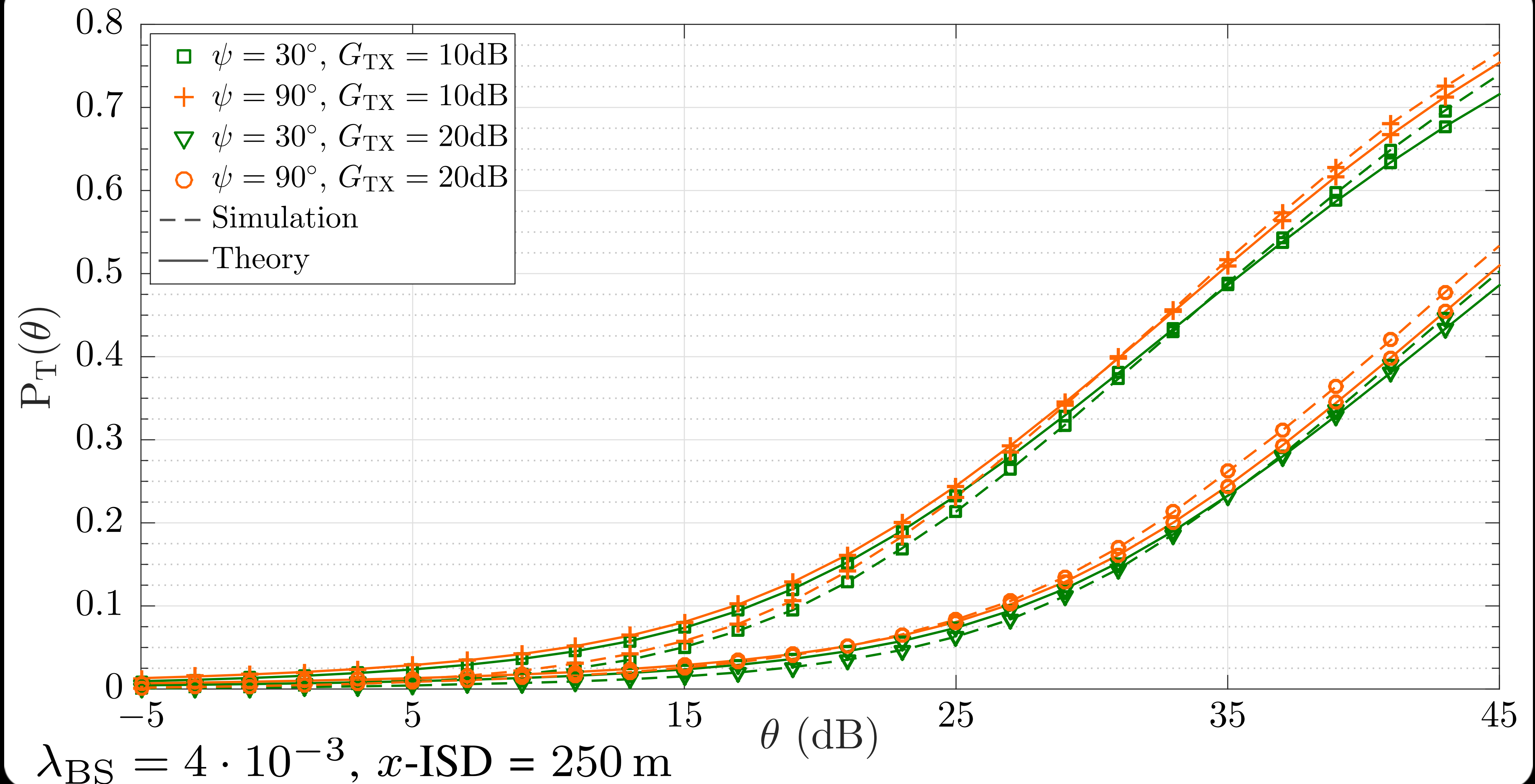


SINR Outage



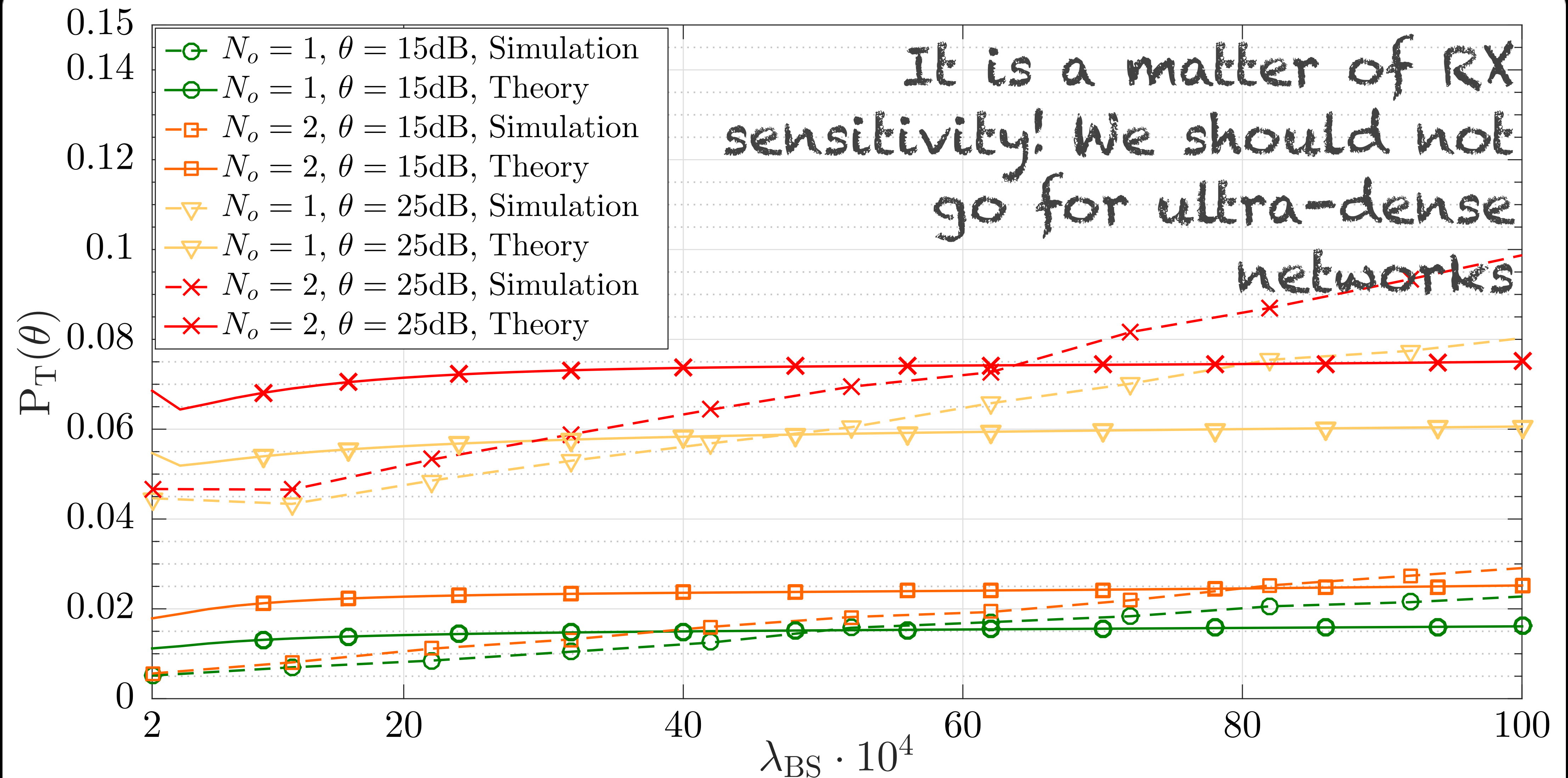


SINR Outage



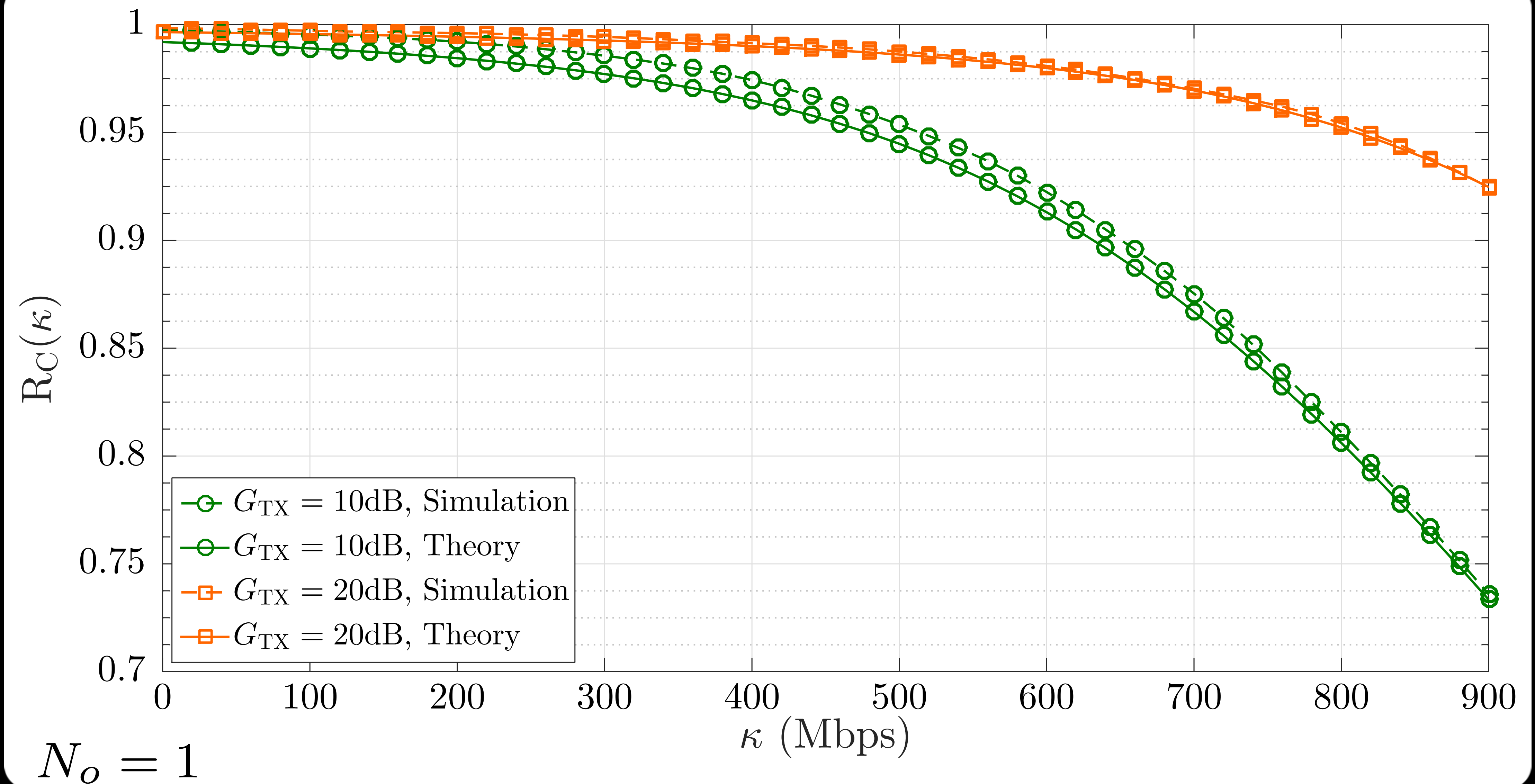


SINR Outage



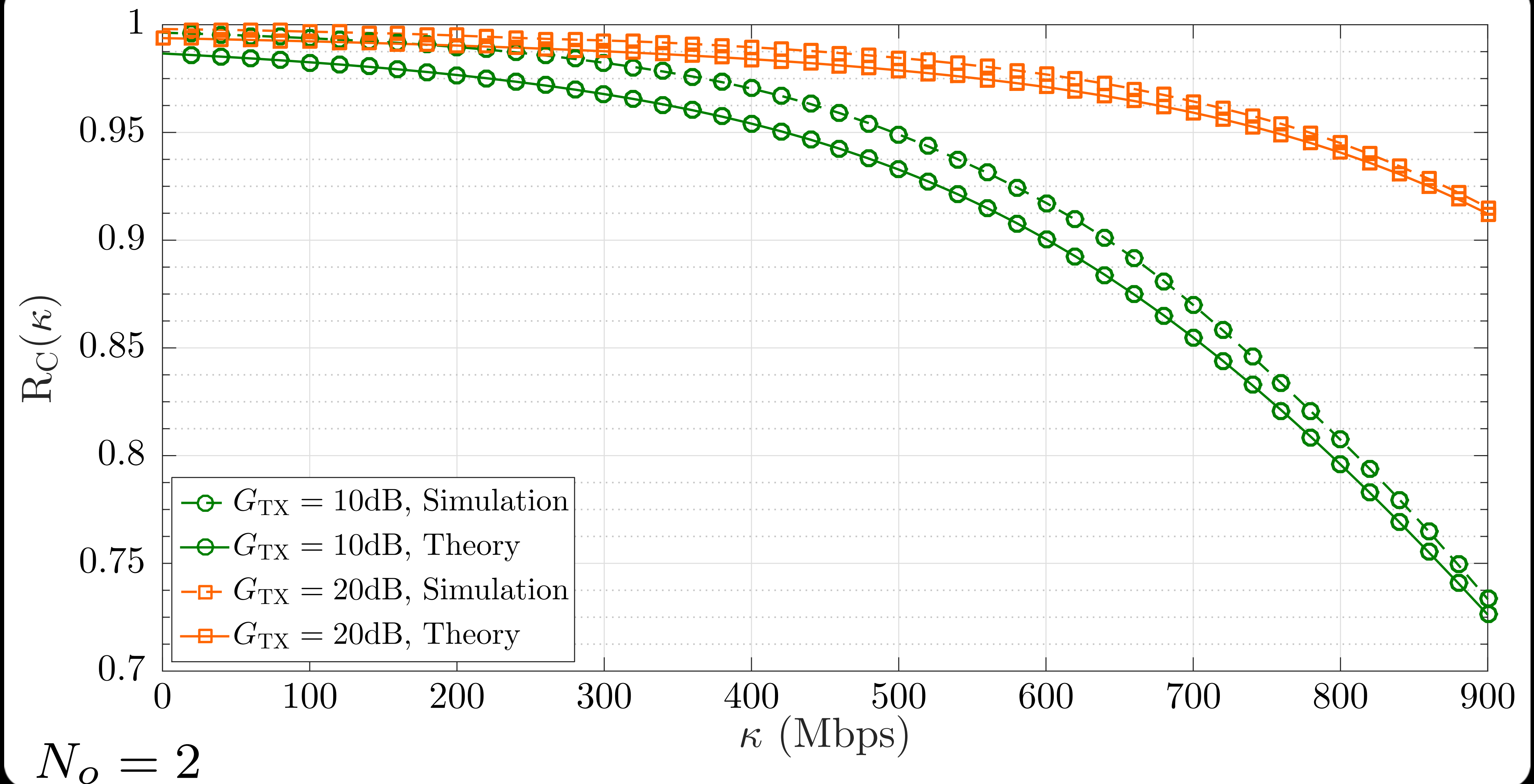


Rate Coverage





Rate Coverage





Conclusions





What Have we seen?

- The probability of being served by a NLOS BS cannot be considered negligible.
- By reducing the antenna beamwidth from 30° to 90° does not necessarily have a disruptive impact on the SINR outage probability, and hence, on the rate coverage probability.
- Differently to what happens in bi-dimensional mmWave cellular networks, the BSs density does not largely affect the network performance.
- Overall, for a fixed SINR threshold, the SINR outage probability tends to be minimized by density values associated to sparse network deployments.



Thanks for your attention!

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